

C of C Math Meet 2003 / Varsity Team Elimination / Round 1

Question 1:

How many positive numbers strictly less than 200 are divisible by either 6 or 10?

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How many positive numbers strictly less than 200 are divisible by either 6 or 10?

Answer: 46

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Question 2:

Write a quadratic equation with positive integer coefficients whose roots are the reciprocals of those of the equation $6x^2 + 11x + 4 = 0$ and whose leading coefficient is the smallest positive integer possible.

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Question 2:

Write a quadratic equation with positive integer coefficients whose roots are the reciprocals of those of the equation $6x^2 + 11x + 4 = 0$ and whose leading coefficient is the smallest positive integer possible.

Answer: $4x^2 + 11x + 6 = 0$

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Question 3:

A rectangle has a perimeter 22 and an area 30. What is the exact value of the length of the rectangle's diagonal?

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A rectangle has a perimeter 22 and an area 30. What is the exact value of the length of the rectangle's diagonal?

Answer: $\sqrt{61}$

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Question 4:

Find p so that the roots of $x^3 + 2px^2 - px + 10 = 0$ are integers in an arithmetic progression.

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Find p so that the roots of $x^3 + 2px^2 - px + 10 = 0$ are integers in an arithmetic progression.

Answer: $p = -3$

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Question 5:

Find all solutions x to the equation:

$$(\ln x)^2 = \ln(x^2).$$

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Find all solutions x to the equation:

$$(\ln x)^2 = \ln(x^2).$$

Answer: $x = 1$ and $x = e^2$

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Question 6:

Find the area of the region which lies between the curves

$$x^2 + (y + 1)^2 = 1 \quad \text{and} \quad x^2 + y^2 = 5$$

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Question 6:

Find the area of the region which lies between the curves

$$x^2 + (y + 1)^2 = 1 \quad \text{and} \quad x^2 + y^2 = 5$$

Answer: 4π

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Question 7:

Solve for x :

$$|x + 2| = |x - 2|.$$

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Solve for x :

$$|x + 2| = |x - 2|.$$

Answer: $x = 0$

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Question 8:

What's the smallest number of people required to ensure that at least 4 have their birthdays in the same month?

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What's the smallest number of people required to ensure that at least 4 have their birthdays in the same month?

Answer: 37

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Question 9:

Your dresser drawer contains 7 red socks and 9 blue socks. You pull two from the drawer at random. What is the probability that the socks match? Give your answer in decimal form.

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Question 9:

Your dresser drawer contains 7 red socks and 9 blue socks. You pull two from the drawer at random. What is the probability that the socks match? Give your answer in decimal form.

Answer: 0.475

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Question 10:

Suppose one randomly removes half of a standard deck of 52 cards without looking at them, and then randomly draws two cards simultaneously from the remaining of the deck. What is the probability that the two cards drawn are a pair of aces? Give your answer in decimal form.

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Question 10:

Suppose one randomly removes half of a standard deck of 52 cards without looking at them, and then randomly draws two cards simultaneously from the remaining of the deck. What is the probability that the two cards drawn are a pair of aces? Give your answer in decimal form.

Answer: 0.004525

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Question 11:

Compute the area of the region enclosed by the graph

$$|2x - 10| + |5y - 10| = 20.$$

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Question 11:

Compute the area of the region enclosed by the graph

$$|2x - 10| + |5y - 10| = 20.$$

Answer: 80

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